

Inconsistencies, Negations and Changes in Ontologies

Giorgos Flouris¹

¹Institute of Computer Science,
FORTH, Heraklion,
Greece
{ggeo, dp}@ics.forth.gr

Zhisheng Huang^{2,3}

²Department of Computer Science,
Vrije Universiteit Amsterdam,
The Netherlands
{huang,holger}@cs.vu.nl

Jeff Z. Pan⁴

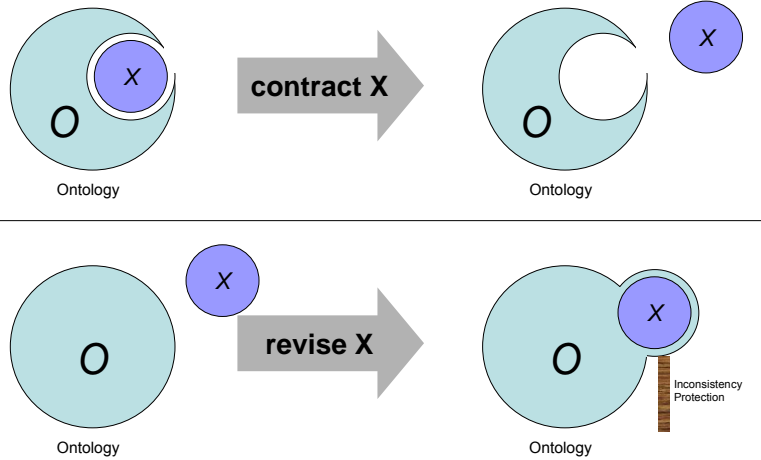
³CWI Amsterdam,
P.O.Box 94079,
The Netherlands

Dimitris Plexousakis¹

⁴Department of Computing Science,
University of Aberdeen,
UK
jpan@csd.abdn.ac.uk

Holger Wache²

Ontology Evolution



Problem: Characteristics of Change Operators

- (B-1) $K-X \subseteq L$ (generalized base closure)
- (B-2) $K-X \subseteq K$ (generalized base inclusion)
- (B-3) If $K \neq X$, then $K-X=K$ (generalized base vacuity)
- (B-4) If $\emptyset \neq X$, then $K-X \neq X$ (generalized base success)
- (B-5) If $X \equiv Y$, then $K-X=K-Y$ (generalized base preservation)
- (B-6) $K \subseteq Cn((K-X) \cup X)$ (generalized base recovery)

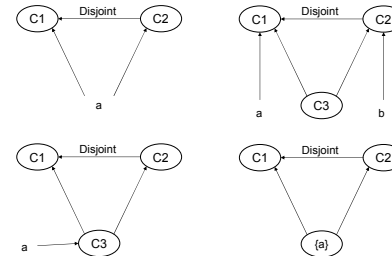
- (B+1) $K+X=Cn(K+X)$
- (B+2) $X \subseteq K+X$
- (B+3) If $Cn(K \cup X) \neq L$ then $K+X=Cn(K \cup X)$
- (B+4) If $Cn(X) \neq L$, then $Cn(K+X) \neq L$
- (B+5) If $Cn(X)=Cn(Y)$, then $K+X=K+Y$
- (B+6) $(K+X) \cap K \neq K-(\neg X)$

BUT Problem:

- Many description logics (including OWL DL) are not AGM-compliant
- Problem: (implicit) **negation** and base recovery postulate

- Belief Revision: 2 x 6 AGM postulates
- AGM postulates describe minimal characteristics for contraction and revision

Incoherency, Inconsistency and Negations



Coherence-Negation

An axiom ψ is said to be a coherence-negation of an axiom ϕ , written $\psi = \sim \phi$, iff

- (Incoherence) $\{\phi, \psi\}$ is **incoherent**,
- (Minimality) There exist no other ψ' such that ψ' satisfies the condition (i), and $Cn(\{\psi'\}) \subset Cn(\{\psi\})$.

Consistency-Negation

An axiom ψ is said to be a consistency-negation of an axiom ϕ , written $\psi = \neg \phi$, iff

- (Inconsistency) $\{\phi, \psi\}$ is **inconsistent**,
- (Minimality) There exist no other ψ' such that ψ' satisfies the condition (i) and $Cn(\{\psi'\}) \subset Cn(\{\psi\})$.

Incoherent Ontology

An ontology O is incoherent iff there exists an unsatisfiable named concept.

Inconsistent Ontology

An ontology O is inconsistent iff it has no interpretation.

New Postulates for Change Operators

- (O-1) $O-X \subseteq O$.
- (O-2) If $O \neq X$, then $O-X=O$.
- (O-3) If $\emptyset \neq X$, then $O-X \neq X$.
- (O-4) If $X \equiv Y$, then $O-X=O-Y$.
- (O-5) If $Cn((O-X) \cup X) \subset Cn(Y \cup X)$ for some $Y \subseteq O$, then $Y \equiv X$ and $\emptyset \neq X$.

- (O+1) $X \subseteq O+X$.
- (O+2) If $Cn(O \cup X) \neq L$, then $O+X=O \cup X$.
- (O+3) If $Cn(X) \neq L$, then $Cn(O+X) \neq L$.
- (O+4) If $X \equiv Y$, then $O+X=O+Y$.
- (O+5) $(O+X) \cap C \equiv O-\neg X$.

Harper: $O-X \equiv Cn(O-\neg X) \cap Cn(O)$
Levi: $O+X \equiv Cn(O-\neg X) \cup Cn(X)$

Results:

- Framework accounts for negation, inconsistency and change for DL-based ontologies for management of dynamic ontologies.
- Proposed negations achieve the Harper identity and Levi identity for ontology change
- Distinction between incoherence and inconsistency provides us two different approaches covering different needs in different application scenarios.